

“A” students work
(without solutions manual)
~ 10 problems/night.

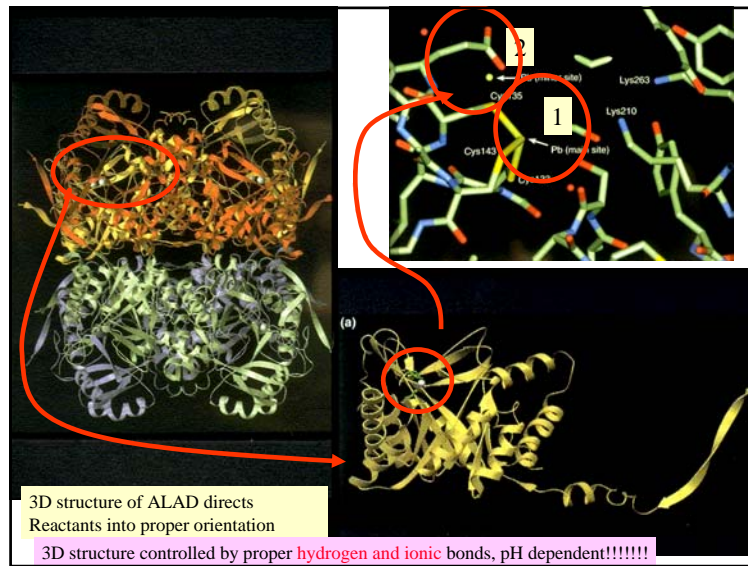
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Office Hours Th&F 2-3:30 pm

**Module #17B:
Acid Base Ionization
Computations**

**I WANT YOU
TO PRACTICE
EVERY DAY!**

To determine if our protein unfolds or not is it sufficient to know the K_a and K_b Values of the functional groups?

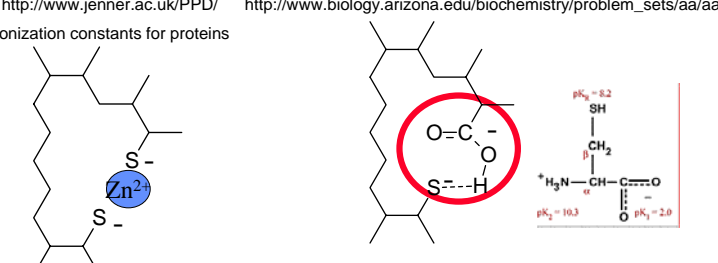


3D structure of ALAD directs Reactants into proper orientation

3D structure controlled by proper hydrogen and ionic bonds, pH dependent!!!!!!

<http://www.jenner.ac.uk/PPD/> http://www.biology.arizona.edu/biochemistry/problem_sets/aa/aa.htm

ionization constants for proteins



$RCOOH_{aq} + H_2O_{\ell} \rightleftharpoons RCOO^{-}_{aq} + H_3O^{+}_{aq}$

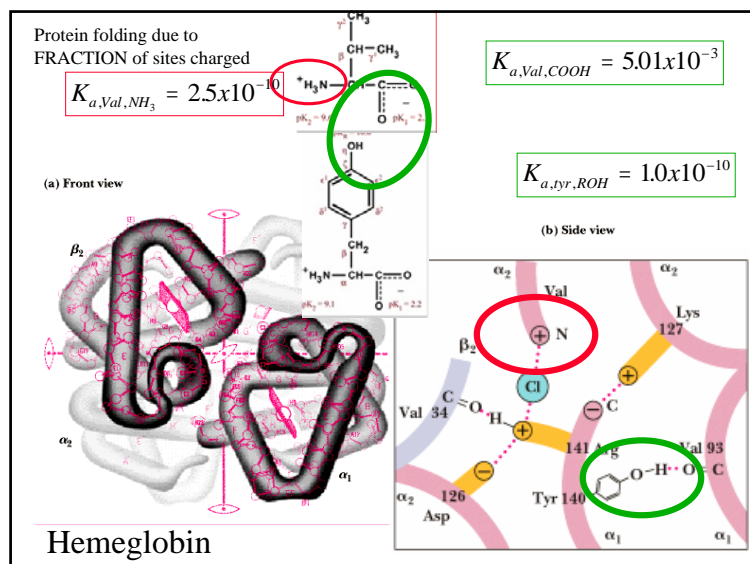
$RSH_{aq} + H_2O_{\ell} \rightleftharpoons RS^{-}_{aq} + H_3O^{+}_{aq}$

R refers to rest of protein

Phosphoenolate carboxylase, human, cys
 $K_a = 7.94 \times 10^{-9}$

cysteine
 $K_{a,COOH} = 1.0 \times 10^{-2}$
 $K_{a,SH} = 6.3 \times 10^{-9}$

Control of protein shape is due to **fraction** of sites charged



% Ionized (dissociated)

$$HA_{aq} \rightleftharpoons H_3O_{aq}^+ + A_{aq}^-$$

$$\% \text{ dissociation} = 100 \left[\frac{\text{amount dissociated (M)}}{\text{initial concentration (M)}} \right]$$

$$\% \text{ dissociation} = 100 \left[\frac{[A_{aq}^-]}{[HA_{aq,initial}]} \right]$$

This seems pretty straight forward

Calculating [A-]
This will require knowing [H₃O_{aq}⁺]

$$HA_{aq} \rightleftharpoons H_3O_{aq}^+ + A_{aq}^-$$

$$K_a = \frac{[A_{aq,eq}^-][H_3O_{aq,eq}^+]}{[HA_{eq,eq}]}$$

AND a new vocabulary for comparing the **solution acidity** from experiment to experiment

K_a and K_b tell us about the possibility Of donating protons, not what the solution Acidity is

Define another comparison number: pH

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pH, pOH, pKa

Chemists are LAZY

To shorten calculations use log

$$\log(ab) = \log(a) + \log(b)$$

$$\log\left(\frac{a}{b}\right) = \log(a) - \log(b) \quad p[x] \equiv -\log[x]$$

$$\log(a)^x = x \log(a)$$

$$\log\left(\frac{1}{a^x}\right) = \log(a^{-x}) = -x \log(a)$$

$$K = \frac{[OH^-]_{eq} [H_3O^+]_{eq}}{[H_2O]^2}$$

Assumption that 55.5 molar is relative unchanged

$$K[H_2O]^2 = [OH^-]_{eq} [H_3O^+]_{eq}$$

$$K[55.55]^2 = [OH^-]_{eq} [H_3O^+]_{eq}$$

$$K[55.55]^2 = K_w = 10^{-14}$$

$$K_w = 10^{-14} = [OH^-]_{eq} [H_3O^+]_{eq}$$

$$K_w = 10^{-14} = [OH^-]_{aq} [H_3O^+]_{aq}$$

$$\log K_w = \log(10^{-14}) = \log[OH^-]_{aq} + \log[H_3O^+]_{aq}$$

$$-14 = \log[OH^-]_{aq} + \log[H_3O^+]_{aq}$$

$$14 = -\log[OH^-]_{aq} + -\log[H_3O^+]_{aq}$$

$$p[x] \equiv -\log[x]$$

$$14 = pOH + pH$$

pH scale runs from 0 to 14

Which is more Acidic?

	acid/base	ave [H ⁺]	pH	pOH	ave [OH ⁻]
base	blood	5.01x10 ⁻⁸	7.3	6.7	1.99x10 ⁻⁷
	saliva	1x10 ⁻⁷	7		
acid	urine	2.51x10 ⁻⁷			
	cow's milk	3.54x10 ⁻⁷			
	cheese	7.94x10 ⁻⁶			

$$pH \equiv -\log[5.01 \times 10^{-8}] = 7.3$$

is slightly larger than 10⁻⁸, so I know it is 7..... something

$$14 - 7.3 = 6.7$$

$$[OH^-] = 10^{-6.7} = 1.995 \times 10^{-7}$$

$$p[x] \equiv -\log[x]$$

$$14 = pH + pOH$$

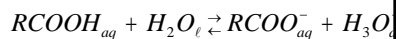
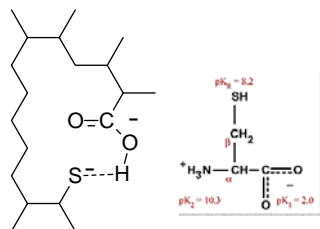
$$x = 10^{-pX}$$

What are the two pK_a s?

$$px = (-1)(\log x)$$

$$pK_a = (-1)(\log(6.3 \times 10^{-9}))$$

$$pK_a = (-1)(-8.2) = 8.2$$



cysteine

$$K_{a,COOH} = 1.0 \times 10^{-2}$$

$$K_{a,SH} = 6.3 \times 10^{-9}$$

What is the K_a of a compound
Whose pK_a is 3.7?

$$x = 10^{-px}$$

$$K_a = 10^{-3.7} = 1.99 \times 10^{-4}$$

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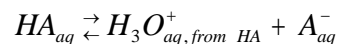
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Calculating [A-]

This will require an equilibrium calculation



$$K_a = \frac{[A^-_{aq,eq}][H_3O^+_{aq,eq}]}{[HA_{aq,eq}]}$$

Generalized Strategy involves comparing K_a s

1. Write down **ALL** possible reactions involving a proton
2. Excluding water, identify all the proton donors as
 1. Strong acid
 - a. Strong electrolyte: HNO_3 , HCl , H_2SO_4 (No Clean Socks)
 - b. Give all strong acid protons to water or alpha dog
 - c. Calculate hydronium conc.
 - d. Calculate pH
 2. Weak Acid
 - a. Identify strongest acid (omega dog, can not hold protons)
 - b. Has **largest K_a** ; smallest charge density anion
 - c. Calculate how many protons omega gives up (equil)
 - d. Calculate pH
 - e. Use to determine what alpha gets

Example Calculations

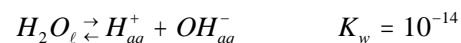
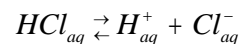
1.HCl

- 2.Acetic acid (vinegar)
- 2.HF
- 3.B(OH)₃ (Boric acid (eye wash))
- 4.Mixture (HF and phenol)
- 5.Mixture (H₂SO₄, HSO₄⁻)
- 6.Triethylamine
- 7.NaAcetate
- 8.Our heme example

Calculate the pH of 0.004 M HCl

Generalized Strategy involves comparing K_as

1. Write down ALL possible reactions involving a proton



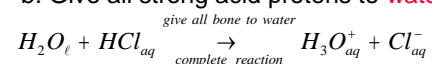
2. Excluding water, identify all the proton donors as

1. Strong acid

- a. Strong electrolyte: HNO₃, HCl, H₂SO₄ (No Clean Socks)

Cl_{aq}⁻ low charge density Omega dog

- b. Give all strong acid protons to **water** or alpha present



- c. Calculate hydronium conc. $H_3O_{aq}^{+} = 0.004 M$
- d. Calculate pH

$$H_3O_{aq}^{+} = 0.004 M$$

Scientific notation allows you to quickly check if Your answer is in the right "ballpark"

$$pH = -\log(4 \times 10^{-3})$$

$$pH = -\log(4) + -\log(10^{-3})$$

$$pH = -\log(4) + -(-3)$$

$$pH = -(0.602) + 3 \quad \text{pH has to be slightly less Than 3}$$

$$pH = 2.39$$

Example Calculations

1.HCl

2.Acetic acid (vinegar)

- 2.HF
- 3.B(OH)₃ (Boric acid (eye wash))
- 4.Mixture (HF and phenol)
- 5.Mixture (H₂SO₄, HSO₄⁻)
- 6.Triethylamine
- 7.NaAcetate
- 8.Our heme example

Example: What is the % ionization of commercial vinegar? The label reads 5% acidity (by weight). Vinegar is acetic acid which has the formula $\text{HC}_2\text{H}_3\text{O}_2$. (CH_3COOH) $K_a = 1.8 \times 10^{-5}$
Density of 5% acetic acid 1.0023 g/mL

1. Write down **ALL** possible reactions involving a proton
 $\text{CH}_3\text{COOH}_{aq} + \text{H}_2\text{O}_\ell \rightleftharpoons \text{H}_3\text{O}_{aq}^+ + \text{CH}_3\text{COO}_{aq}^- \quad K_a = 1.8 \times 10^{-5}$
 $\text{H}_2\text{O}_\ell \rightleftharpoons \text{H}_{aq}^+ + \text{OH}_{aq}^- \quad K_w = 10^{-14}$
2. Excluding water, identify all the proton donors as
 1. Strong acid
 a. Strong electrolyte: HNO_3 , HCl , H_2SO_4 (None)
 2. Weak Acid:
 $\text{CH}_3\text{COOH}_{aq} + \text{H}_2\text{O}_\ell \rightleftharpoons \text{H}_3\text{O}_{aq}^+ + \text{CH}_3\text{COO}_{aq}^- \quad K_a = 1.8 \times 10^{-5}$
 a. Calculate how many protons omega gives up (equil)

Example: What is the % ionization of commercial vinegar? The label reads 5% acidity (by weight). Vinegar is acetic acid which has the formula $\text{HC}_2\text{H}_3\text{O}_2$. (CH_3COOH) $K_a = 1.8 \times 10^{-5}$
Density of 5% acetic acid 1.0023g/mL

Know	Don't Know
% by wt. $K_a = 1.8 \times 10^{-5}$	Need the initial molarity need the final dissociation
$\left(\frac{5g_{\text{acetic acid}}}{100g_{\text{solution}}}\right) 100g_{\text{solution}} = 5g_{\text{acetic acid}}$ $\left(5g_{\text{acetic acid}}\right) \left(\frac{1\text{mole}_{\text{acetic acid}}}{2(12) + 4(1) + 2(16)}\right) = \left(5g_{\text{acetic acid}}\right) \left(\frac{1\text{mole}_{\text{acetic acid}}}{60g_{\text{acetic acid}}}\right) = \frac{0.083\text{mole}}{0.0997L} = 0.835M$ $\left(100g_{\text{solution}}\right) \left(\frac{1\text{mL}_{\text{solution}}}{1.0023g_{\text{solution}}}\right) \left(\frac{1L}{10^3\text{mL}}\right) = \frac{0.0997L}{0.0997L} = 0.835M$	

$[\text{HC}_2\text{H}_3\text{O}_2] = 0.8355M$ Why complicate this situation by adding in 10^{-7} When we get rid off it with an assumption?
 Because it creates a habit necessary of multiple rx

	H_2O	OH^-	H^+
	55.5	10^{-7}	10^{-7}
stoic	$\text{HC}_2\text{H}_3\text{O}_2$	$\text{C}_2\text{H}_3\text{O}_2^-$	H^+
conc. init	1	1	1
[Init]	5%	0	10^{-7}
Change	0.8355	0	10^{-7}
Assume	-x	+x	+x
[Equil]	0.8355 >>> x	+x	$10^{-7} \ll x$

What is the % ionization of commercial vinegar? The label reads 5% acidity (by weight). Density of 5% acetic acid is 1.0023 g/mL. Vinegar is acetic acid which has the formula $\text{HC}_2\text{H}_3\text{O}_2$. (CH_3COOH) $K_a = 1.8 \times 10^{-5}$

$$K_a = \frac{(x)(10^{-7} + x)}{[HA]_{\text{init}} - x} \quad 1.8 \times 10^{-5} = \frac{x^2}{0.8355}$$

	HA	A	H^+
Assume	0.8355 >>> x	+x	$10^{-7} \ll x$
		$0.8355 - x \approx 0.8355$ (5% error)	
	$0.8355(K_a) = x^2$	0.835500	
	$\sqrt{0.8355(K_a)} = x$	0.003878 ($\frac{0.003878}{0.831622}$) ¹⁰⁰ = 0.46%	
	$x = \sqrt{(1.8 \times 10^{-5})(0.8355)} = 0.003878$	0.831622	
Check:	$x + 10^{-7} \approx x$ (5% error)		Original sig figs were = 0.83
	0.0038780		So if we round to 2 sig fig, have
	+ 0.0000001		Same answer
	0.0039779		
	Sig figs ($\frac{0.0000001}{0.0039779}$) ¹⁰⁰ = 0.002%		
			$\text{pH} = (-1)[\log(0.0038778)] = (-1)(-2.41) = 2.41$

$$\% \text{ dissociation} = 100 \left[\frac{[A^-]_{eq}}{[HA]_{aq, initial}} \right]$$

$$\left(\frac{0.003878}{0.835} \right) 100 = 0.46\%$$

What is the % ionization of commercial vinegar? The label reads 5% acidity (by weight). Density of 5% acetic acid is 1.0023 g/mL. Vinegar is acetic acid which has the formula HC₂H₃O₂. (CH₃COOH) K_a = 1.8x10⁻⁵

How does % dissociation or ionization vary with concentration?

[Acetic Acid]	% ionization	
1.00 M	0.42%	
0.835M	0.46%	
0.1 M	1.3%	Observations?

% ionization increases with the lower molarity.

Why should this be so?

What is the % ionization of commercial vinegar? The label reads 5% acidity (by weight). Density of 5% acetic acid is 1.0023 g/mL. Vinegar is acetic acid which has the formula HC₂H₃O₂. (CH₃COOH) K_a = 1.8x10⁻⁵

$$K_a = \frac{[H^+][A^-]}{[HA]}$$

Dilute by 10 (make less concentrated):

$$Q = \frac{\left(\frac{[H^+]}{10} \right) \left(\frac{[A^-]}{10} \right)}{\frac{[HA]}{10}} = \frac{[H^+][A^-]}{[HA]10} <, =, > K?$$

What does this tell us, if anything?

We have too many reactants, need to shift to the **right**, or dissociate some more.

general rule of thumb: dilution gives more dissociation.

Example Calculations

- 1.HCl
- 2.Acetic acid (vinegar)
- 3.HF**
- 4.B(OH)₃ (Boric acid (eye wash)) (students Do this one yourself)
- 5.Mixture (HF and phenol)
- 6.Mixture (H₂SO₄, HSO₄⁻)
- 7.Triethylamine
- 8.NaAcetate
- 9.Our heme example

Calculate the F- of a solution of 1.00 M HF.
 $K_a = 7.2 \times 10^{-4}$

1. Write down ALL possible reactions involving a proton

$$HF_{aq} \rightleftharpoons H_{aq,F}^+ + F_{aq}^- \quad K_a = 7.2 \times 10^{-4}$$

$$H_2O_l \rightleftharpoons H_{aq}^+ + OH_{aq}^- \quad K_w = 10^{-14}$$

2. Excluding water, identify all the proton donors as

1. Strong acid

a. Strong electrolyte: HNO₃, HCl, H₂SO₄ (No Clean Socks)

No Strong Acids (SA)

2. Weak Acid

a. Identify strongest acid (omega dog, can not hold protons)

b. Has **largest K_a**; smallest charge density anion

$$HF_{aq} \rightleftharpoons H_{aq,F}^+ + F_{aq}^- \quad K_a = 7.2 \times 10^{-4}$$

c. Calculate how many protons omega gives up (equil)

	H ₂ O	H ⁺	OH ⁻
	55.5	10 ⁻⁷	10 ⁻⁷
	HF _(aq)	H ⁺ _{from HF}	F ⁻
stoic.	1	1	1
Init	1.0	10 ⁻⁷	0
Change	-x	+x	+x
Assum	1 >> x	10 ⁻⁷ << x	
Equil	1	x	x

	HF _(aq)	H ⁺ _{from HF}	F ⁻
Init	1.0	10 ⁻⁷	0
Change	-x	+x	+x
Assum	1 >> x	10 ⁻⁷ << x	
Equil	1	x	x

$K_a = \frac{(x)(x + 10^{-7})}{1 - x} \approx \frac{x^2}{1}$ Check assumptions

$1(K_a) = x^2$ $1 - 7.2 \times 10^{-2} \approx 1?$ $2.7 \times 10^{-2} + 10^{-7} \approx 2.7 \times 10^{-2}?$

	1.00	0.027
	- 0.027	+ 0.0000001
	0.983	0.0270001

Sig fig is here

0.983 = 1 0.0270001 = 0.027

Calculate the pH of a solution of 1.00 M HF.
 $K_1 = 7.2 \times 10^{-4}$

	HF _(aq)	H ⁺ _{from HF}	F ⁻
Init	1.0	10 ⁻⁷	0
Change	-x	+x	+x
Assum	1 >> x	10 ⁻⁷ << x	
Equil	1	x	x

$x = 2.7 \times 10^{-2}$

$x = [F^-] = 2.7 \times 10^{-2}$

$pH = (-1) [\log(2.7 \times 10^{-2})] = (-1)(-1.568) = 1.6$

Calculate the F- of a solution of 1.00 M HF.
 $K_1 = 7.2 \times 10^{-4}$

Example: Boric acid is commonly used in eyewash solutions to neutralize bases splashed in the eye. It acts as a monoprotic acid, but the dissociation reaction looks different. Calculate the pH of a 0.75 M solution of boric acid, and the concentration of $B(OH)_4^-$.

$$B(OH)_{3,aq} + H_2O_{\ell} \rightleftharpoons B(OH)_{4,aq}^- + H_3O_{aq}^+ \quad K_a = 5.8 \times 10^{-10}$$

1. Write down **ALL** possible reactions involving a proton

$$B(OH)_{3,aq} + H_2O_{\ell} \rightleftharpoons B(OH)_{4,aq}^- + H_3O_{aq}^+ \quad K_a = 5.8 \times 10^{-10}$$

$$H_2O_{\ell} \rightleftharpoons H_{aq}^+ + OH_{aq}^- \quad K_w = 10^{-14}$$

2. Identify proton donors

1. strong acids: No Clean Socks? No SA
2. Weak acids: $B(OH)_3$

Students do
This on your own

Set up ICE chart

	H_2O	\rightleftharpoons	OH^-	H^+
	55.5		10^{-7}	10^{-7}
	$B(OH)_3 + H_2O \rightleftharpoons B(OH)_4^- + H^+$			
stoic	1	n.a.	1	1
[Init]	0.75		0	10^{-7}
Change	-x		+x	+x
Assume	$0.75 \gg x$		x	$10^{-7} \ll x$
Equil	0.75		x	x

$$K_a = \frac{x(x + 10^{-7})}{[HA]_{init} - x} \approx \frac{x^2}{[HA]_{init}} \quad \sqrt{(5.8 \times 10^{-10})0.75} = x = 2.1 \times 10^{-5}$$

$$5.8 \times 10^{-10} = \frac{x^2}{0.75}$$

$B(OH)_3 + H_2O \rightleftharpoons B(OH)_4^- + H^+ \quad K_a = 5.8 \times 10^{-10}$
Calculate the pH of a 0.75 M solution of boric acid.

	$B(OH)_3 + H_2O$	$B(OH)_4^- + H^+$
[Init]	0.75	0 10^{-7}
Change	-x	+x +x
Assume	$0.75 \gg x$	x $10^{-7} \ll x$
Equil	0.75	x x

$$\sqrt{(5.8 \times 10^{-10})0.75} = x = 2.1 \times 10^{-5}$$

$0.75 - x \stackrel{5\% \text{ error}}{\approx} 0.75?$ $x = [B(OH)_4^-] = 2.1 \times 10^{-5}$
yes

$x + 10^{-7} \stackrel{5\% \text{ error}}{\approx} x?$ $x = [H^+] = 2.1 \times 10^{-5}$
0.000021

$$pH = (-1) \log(2.1 \times 10^{-5}) = 4.68 = 4.7$$

+ 0.0000001

0.0000211

↑ Sig fig

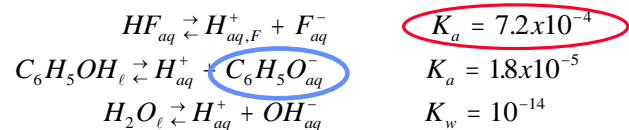
Students do
This on your own

$B(OH)_3 + H_2O \rightleftharpoons B(OH)_4^- + H^+ \quad K_a = 5.8 \times 10^{-10}$
Calculate the pH of a 0.75 M solution of boric acid.

- Example Calculations
1. HCl
 2. Acetic acid (vinegar)
 3. HF
 4. $B(OH)_3$ (Boric acid (eye wash)) (students Do this one yourself)
 5. Mixture (HF and phenol)
 6. Mixture (H_2SO_4 , HSO_4^-)
 7. Triethylamine
 8. NaAcetate
 9. Our heme example

Mixtures of Acids Calculate the pH of a solution that contains 1.0 M HF and 1.0 M HOC_6H_5 . Calculate the conc. of $-\text{OC}_6\text{H}_5$ at this concentration.

1. Write down ALL possible reactions involving a proton



2. Excluding water, identify all the proton donors as

1. Strong acid **NONE**
2. Weak Acid

Identify strongest acid (omega dog, can not hold protons)
Has **largest K_a** ; smallest charge density anion
Calculate how many protons omega gives up (equil)
Calculate pH (Use to determine what alpha gets)

HF will control the proton concentration, but
Should include all possible sources to remind ourselves.

	H_2O	\rightleftharpoons	OH^-	H^+
	55.5		10^{-7}	10^{-7}
	HF + H_2O	\rightleftharpoons	F^- +	H^+
stoic	1		1	1
[Init]	1.0		0	10^{-7}
Change	-x		+x	+x
Assume	$1.0 \gg x$		x	$10^{-7} \ll x$
Equil	1.0		x	x

$$K_a = \frac{x(x + 10^{-7})}{[HA]_{init} - x} \approx \frac{x^2}{[HA]_{init}} \quad 7.2 \times 10^{-4} = \frac{x^2}{1} \quad \sqrt{7.2 \times 10^{-4}} = x = 2.7 \times 10^{-2}$$

HF	$\text{H}^+ + \text{F}^-$	$K_a = 7.2 \times 10^{-4}$
HOC_6H_5	$\text{H}^+ + -\text{OC}_6\text{H}_5$	$K_a = 1.8 \times 10^{-5}$

Calculate the pH of a solution that contains 1.0 M HF and 1.0 M HOC_6H_5 . Calculate the conc. of $-\text{OC}_6\text{H}_5$ at this concentration.

	HF	+ H_2O	\rightleftharpoons	F^-	+ H^+
stoic	1	n.a.		1	1
[Init]	1.0			0	10^{-7}
Change	-x			+x	+x
Assume	$1.0 \gg x$			x	$10^{-7} \ll x$
Equil	1.0			x	x

$$\sqrt{7.2 \times 10^{-4}} = x = 2.7 \times 10^{-2}$$

Check assumptions:

$$1 - 2.7 \times 10^{-2} \stackrel{5\% \text{ error}}{\approx} 1? \quad \frac{1.0 - 0.027}{1.0} = 0.973$$

Sig fig = 1.0

$$2.7 \times 10^{-2} + 10^{-7} \stackrel{5\% \text{ error}}{\approx} 2.7 \times 10^{-2}?$$

$$\frac{0.027}{1.0} + 0.0000001 = 0.0270001$$

Sig fig = 0.027

	HF	+ H_2O	\rightleftharpoons	F^-	+ H^+
stoic	1	n.a.		1	1
[Init]	1.0			0	10^{-7}
Change	-x			+x	+x
Assume	$1.0 \gg x$			x	$10^{-7} \ll x$
Equil	1.0			x	x
	1.0			2.7×10^{-2}	2.7×10^{-2}

$$\sqrt{7.2 \times 10^{-4}} = x = 2.7 \times 10^{-2}$$

$$[H^+] = x = 2.7 \times 10^{-2}$$

Calculate the pH of a solution that contains 1.0 M HF and 1.0 M HOC_6H_5 . Calculate the conc. of $-\text{OC}_6\text{H}_5$ at this concentration.

	HF	+	H₂O	\rightleftharpoons	F⁻	+	H⁺	
stoic	1		n.a.		1		1	
[Init]	1.0				0		10⁻⁷	
Change	-x				+x		+x	
Assume	1.0 >> x				x		10⁻⁷ << x	
Equil	1.0				2.7x10⁻²		2.7x10⁻²	

	C₆H₅OH	+	H₂O	\rightleftharpoons	C₆H₅O⁻	+	H⁺	
stoic	1		n.a.		1		1	
[Init]	1.0				0		2.7x10⁻²	
Change	-x				+x		+x	
Assume	1.0 >> x				x		x << 2.7x10⁻²	
Equil	1.0				x		2.7x10⁻²	

	C₆H₅OH	+	H₂O	\rightleftharpoons	C₆H₅O⁻	+	H⁺	
stoic	1		n.a.		1		1	
[Init]	1.0				0		2.7x10⁻²	
Change	-x				+x		+x	
Assume	1.0 >> x				x		x << 2.7x10⁻²	
Equil	1.0				x		2.7x10⁻²	

$$C_6H_5OH + H_2O \rightleftharpoons H_3O_{aq}^+ + C_6H_5O_{aq}^- \quad K_a = 1.8 \times 10^{-5}$$

$$K_a = 1.8 \times 10^{-5} = \frac{[H_3O_{aq}^+][C_6H_5O_{aq}^-]}{[C_6H_5OH_{eq}]} \quad [2.7 \times 10^{-2}] + x \approx [2.7 \times 10^{-2}]?$$

$$100 \left(\frac{6.66 \times 10^{-4}}{2.7 \times 10^{-2}} \right) = 2.46\%$$

$$K_a = 1.8 \times 10^{-5} = \frac{(2.7 \times 10^{-2} + x)x}{1-x} \approx \frac{(2.7 \times 10^{-2})x}{x} \approx 2.7 \times 10^{-2}$$

$$x = \frac{1.8 \times 10^{-5}}{2.7 \times 10^{-2}} = 6.66 \times 10^{-4}$$

Calculate the pH of a solution that contains 1.0 M HF and 1.0 M HOC₆H₅. Calculate the conc. of -OC₆H₅ at this concentration.

- Example Calculations
- HCl
 - Acetic acid (vinegar)
 - HF
 - B(OH)₃ (Boric acid (eye wash)) (students Do this one yourself)
 - Mixture (HF and phenol)
 - Mixture (H₂SO₄, HSO₄⁻)**
 - Triethylamine
 - NaAcetate
 - Our heme example

- Example: calculate the pH of 0.0010 M sulfuric acid
- Write down **ALL** possible reactions involving a proton

$$H_2SO_{4,aq} + H_2O \rightleftharpoons HSO_{4,aq}^- + H_3O_{aq}^+ \quad K_a = \text{large}$$

$$HSO_{4,aq}^- + H_2O \rightleftharpoons H_3O_{aq}^+ + SO_{4,aq}^{2-} \quad K_a = 1.2 \times 10^{-2}$$

$$H_2O \rightleftharpoons H_{aq}^+ + OH_{aq}^- \quad K_w = 10^{-14}$$
 - Excluding water, identify all the proton donors as
 - Strong acid
 - Strong electrolyte: HNO₃, HCl, H₂SO₄ (No Clean Socks)
$$H_2SO_{4,aq} + H_2O \rightleftharpoons HSO_{4,aq}^- + H_3O_{aq}^+ \quad K_a = \text{large}$$
 - Give all strong acid protons to water or **alpha dog**

1	Pure Water	H ₂ O	OH ⁻	H ⁺	
	Control/complete	H ₂ SO ₄	HSO ₄ ⁻	H ⁺	
2	stoic.	1	1	1	
	[init]	.0010	0	10 ⁻⁷	
	complete	0	0.0010	0.0010+10 ⁻⁷	
		0	0.0010	0.0010	
3	stoic.		HSO ₄ ⁻	H ⁺	SO ₄ ²⁻
	[Init]		0.0010	0.0010	0
	Change		-x	+x	+x
	Assume?		0.0010 > x	0.0010 > x	+x
	[Equil]		0.0010	0.0010	x

$K_{a2} = \frac{[H_3O^+_{aq,eq}][SO_4^{2-}_{aq,eq}]}{[HSO_4^-_{aq,eq}]}$
 $K_{a2} = 1.2 \times 10^{-2} = \frac{[0.001 + x][x]}{[0.001] - x} \stackrel{5\% \text{ error}}{\approx} \frac{0.001x}{0.001} = x$

$K_{a2} = 1.2 \times 10^{-2} = x = [SO_4^{2-}]$

$1.2 \times 10^{-2} + 0.001 \stackrel{5\% \text{ error}}{\approx} 0.001?$ **NO!**

Example: calculate the pH of 0.0010 M sulfuric acid; $K_{a2} = 1.2 \times 10^{-2}$

$1.2 \times 10^{-2} + 0.001 \stackrel{5\% \text{ error}}{\approx} 0.001?$
 $\left(\frac{1.2 \times 10^{-2}}{0.001}\right) 100 = 1200\% \text{ error!}$

Here is our first example in which we can not make assumptions

stoic.	HSO ₄ ⁻	H ⁺	SO ₄ ²⁻
	1	1	1
[Init]	0.0010	0.0010	0
Change	-x	+x	+x
Assume?	0.001 > x	0.001 > x	+x
[Equil]	0.001-x	0.001+x	x

$K_{a2} = 1.2 \times 10^{-2} = \frac{[0.001 + x][x]}{[0.001 - x]}$
 $(1.2 \times 10^{-2})(0.001 - x) = (0.001 + x)x$

$1.2 \times 10^{-5} - 1.2 \times 10^{-2}x = 0.001x + x^2$

$x^2 + 0.001x + 1.2 \times 10^{-2}x - 1.2 \times 10^{-5} = 0$

$x^2 + 0.013x - 1.2 \times 10^{-5} = 0$

Example: calculate the pH of 0.0010 M sulfuric acid; $K_{a2} = 1.2 \times 10^{-2}$

$x^2 + 0.013x - 1.2 \times 10^{-5} = 0$

$x = \frac{-0.013 \pm \sqrt{(0.013)^2 - 4(1)(-0.000012)}}{2(1)}$

$x = \frac{-0.013 \pm \sqrt{2.17 \times 10^{-4}}}{2}$

$x = \frac{-0.013 \pm 0.0147}{2}$

$x = 8.65 \times 10^{-4}$

$[SO_4^{2-}] = x$

$[H^+] = 0.001 + 0.000865 = 0.001865$

$pH = -\log(0.001865) = 2.73$

$ax^2 + bx + c = 0$

$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

-Solution gives a neg Number which is not allowed

Successive Approximations (iterations)

Alternative Strategy to going to "exact equil. Expression"

ITERATIVE SOLUTIONS

Why? – because the real body or real world is much too complex to always be able to Find an exact equilibrium expression

Calculate proton concentration of 0.100 M HNO₂ using the **iterative method** ($K_a=6.0 \times 10^{-4}$)

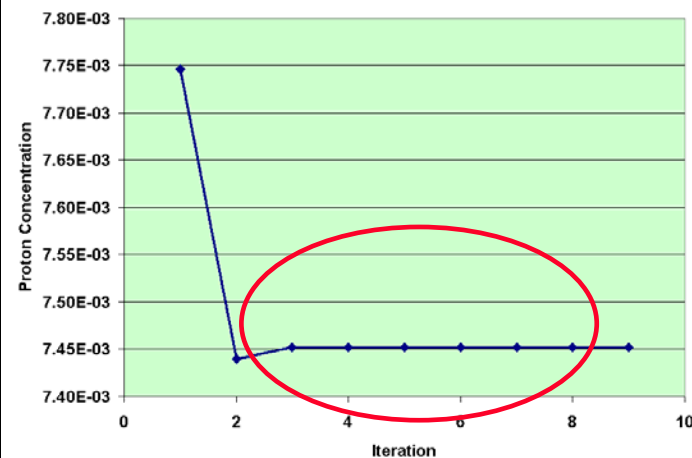
1	Pure Water	H ₂ O 55.5	OH ⁻ 10 ⁻⁷	H ⁺ 10 ⁻⁷
		HNO ₂	NO ₂	H ⁺
2	stoic.	1	1	1
	[Init]	0.100	0	10 ⁻⁷
	Change	-x	+x	+x
	Assume	0.100 >> x	x	x >> 10 ⁻⁷
	[Equil]	0.100	x	x
	Calc 1			7.7x10 ⁻³
3	New Equil	0.100 - 7.7x10 ⁻³	x''	x''
	Calc 2			7.44x10 ⁻³
4	New New Equil	0.100 - 7.44x10 ⁻³	x'''	x'''
	Calc 3			7.45x10 ⁻³


$$K_a = \frac{x^2}{[HA_{eq}]} \quad \sqrt{K_a [HA_{eq}]} = x$$

$$x'' = \sqrt{(6.0 \times 10^{-4})(0.1 - 7.7 \times 10^{-3})} = \sqrt{(6.0 \times 10^{-4})(0.0923)}$$

$$x = \sqrt{(6.0 \times 10^{-4})(0.1)} = 7.7 \times 10^{-3} \quad x'' = \sqrt{5.538 \times 10^{-5}} = 7.44 \times 10^{-3}$$

Converging, plausible answer for iterative method: 0.100 M HNO₂, $K_a=6.0 \times 10^{-4}$





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Module #17B:
Acid Base Ionization
Computations


Weak Bases

Example Calculations

1. HCl
2. Acetic acid (vinegar)
3. HF
4. B(OH)₃ (Boric acid (eye wash)) (students Do this one yourself)
5. Mixture (HF and phenol)
6. Mixture (H₂SO₄, HSO₄⁻)
- 7. Triethylamine**
8. NaAcetate
9. Our heme example

Calculation with Weak Base				
Calc. the [OH], [H], and pH of 0.20 M solns of triethylamine, $K_b = 4.0 \times 10^{-4}$				
1		H_2O	H^+	OH^-
		55.5	10^{-7}	10^{-7}
	B	H_2O	BH^+	OH^-
2	stoic	1	1	1
	[Init]	0.20	0	10^{-7}
	Change	-x	+x	+x
	Assum	$0.20 \gg x$	x	$10^{-7} < x$
	Equil	0.20	x	x
Calc. the [OH], [H], and pH of 0.20 M solns of triethylamine, $K_b = 4.0 \times 10^{-4}$				

1		H_2O	H^+	OH^-
		55.5	10^{-7}	10^{-7}
	B	H_2O	BH^+	OH^-
2	stoic	1	1	1
	[Init]	0.20	0	10^{-7}
	Change	-x	+x	+x
	Assum	$0.20 \gg x$	x	$10^{-7} < x$
	Equil	0.20	x	x
$K_b = 4.0 \times 10^{-4} = \frac{x(x + 10^{-7})}{0.2 - x} \approx \frac{x^2}{0.2}$				
$\sqrt{(4.0 \times 10^{-4}) \cdot 0.2} = x = 8.94 \times 10^{-3}$				
$8.94 \times 10^{-3} + 10^{-7} \stackrel{5\% \text{ error}}{\approx} 8.94 \times 10^{-3} ?$				
$0.20 - 8.94 \times 10^{-3} \stackrel{5\% \text{ error}}{\approx} 0.2 ?$				
Calc. the [OH], [H], and pH of 0.20 M solns of triethylamine, $K_b = 4.0 \times 10^{-4}$				
$x = [OH^-] = 8.94 \times 10^{-3}$ $pOH = (-1) \log(0.00894) = 2.048$ $pH = 14 - 2.048 = 11.95$				



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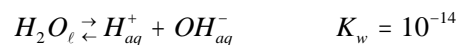
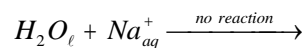
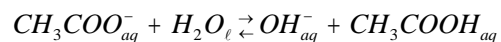
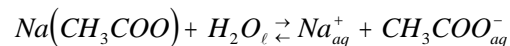
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Module #17B:
Acid Base Ionization
Computations

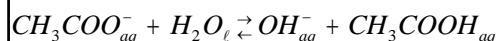
Salts

- Example Calculations
1. HCl
 2. Acetic acid (vinegar)
 3. HF
 4. $B(OH)_3$ (Boric acid (eye wash)) (students Do this one yourself)
 5. Mixture (HF and phenol)
 6. Mixture (H_2SO_4 , HSO_4^-)
 7. Triethylamine
 - 8. NaAcetate**
 9. Our heme example

Write all reactions involving protons, hydroxides

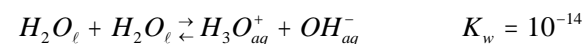


Determine who is omega and will donate



Hmm, a slight problem – we don't know K_b

If we place Na acetate in solution (to make a 0.1 M solution) what are the main species present? What will be the pH of the solution? $K_a = 1.8 \times 10^{-5}$



$$K_w = K_a K_b$$

$$\frac{10^{-14}}{1.8 \times 10^{-5}} = K_b = 5.55 \times 10^{-10}$$

If we place Na acetate in solution (to make a 0.1 M solution) what are the main species present? What will be the pH of the solution? $K_a = 1.8 \times 10^{-5}$

$$K_b = 5.55 \times 10^{-10}$$

1		H_2O	H^+	OH^-
		55.5	10^{-7}	10^{-7}
2		$CH_3COO^- + H_2O = CH_3COOH + OH^-$		
	stoich	1	1	1
	[Init]	0.1	0	10^{-7}
	Change	-x	+x	$10^{-7} + x$
	Sum	0.1-x	0+x	$10^{-7} + x$
	Assume	$x \ll \ll 0.1$		$x \gg \gg 10^{-7}$
	[Equil]	0.1	x	x

If we place Na acetate in solution (to make a 0.1 M solution) what are the main species present? What will be the pH of the solution? $K_a = 1.8 \times 10^{-5}$

	$K_b = 5.55 \times 10^{-10}$	$CH_3COO^- + H_2O = CH_3COOH + OH^-$		
	stoich	1	1	1
	[Init]	0.1	0	10^{-7}
	Change	-x	+x	$10^{-7} + x$
	Sum	0.1-x	0+x	$10^{-7} + x$
	Assume	$x \ll \ll 0.1$		$x \gg \gg 10^{-7}$
	[Equil]	0.1	x	x

$$5.55 \times 10^{-10} = \frac{[OH_{aq,eq}^-][CH_3COOH_{aq,eq}]}{[CH_3COO_{aq,eq}^-]} = \frac{(x + 10^{-7})x}{0.1 - x} \approx \frac{x^2}{0.1}$$

$$5.55 \times 10^{-10} = \frac{x^2}{0.1} \quad 0.1 - 7.45 \times 10^{-6} \stackrel{5\% \text{ error}}{\approx} 0.1? \quad \text{No}$$

$$\sqrt{(5.55 \times 10^{-10})0.1} = x \quad \text{yes}$$

$$x = 7.45 \times 10^{-6}$$

If we place Na acetate in solution (to make a 0.1 M solution) what are the main species present? What will be the pH of the solution? $K_a = 1.8 \times 10^{-5}$

$\text{CH}_3\text{COO}^- + \text{H}_2\text{O} = \text{CH}_3\text{COOH} + \text{OH}^-$			
stoich	1	1	1
[Init]	0.1	0	10^{-7}
Change	-x	+x	$10^{-7} + x$
Sum	0.1-x	0+x	$10^{-7} + x$
Assume	$x \ll 0.1$		$x \gg 10^{-7}$
[Equil]	0.1	x	x
Equil new	0.1-x	x	$x + 10^{-7}$

$K_b = 5.55 \times 10^{-10} = \frac{[x][x + 10^{-7}]}{[0.1 - x]}$
 $(5.55 \times 10^{-10})(0.1 - x) = [x][x + 10^{-7}] = x^2 + (10^{-7})x$

If we place Na acetate in solution (to make a 0.1 M solution) what are the main species present? What will be the pH of the solution? $K_a = 1.8 \times 10^{-5}$

$$(5.55 \times 10^{-10})(0.1 - x) = [x][x + 10^{-7}] = x^2 + (10^{-7})x$$

$$5.55 \times 10^{-11} - (5.55 \times 10^{-10})x = x + (10^{-7})x$$

$$x^2 + (10^{-7})x + (5.55 \times 10^{-10})x - 5.55 \times 10^{-11} = 0$$

$$x^2 + (1.00555 \times 10^{-7})x - 5.55 \times 10^{-11} = 0$$


$$x = \frac{-1.00555 \times 10^{-7} \pm \sqrt{(1.00555 \times 10^{-7})^2 - 4(1)(-5.55 \times 10^{-11})}}{2(1)} \quad ax^2 + bx + c = 0$$

$$x = \frac{-1.00555 \times 10^{-7} \pm \sqrt{1.01103 \times 10^{-14} + 2.22 \times 10^{-10}}}{2}$$

$$x = \frac{-1.00555 \times 10^{-7} \pm \sqrt{2.22 \times 10^{-10}}}{2}$$

$$x = \frac{-1.00555 \times 10^{-7} \pm 1.49 \times 10^{-5}}{2} = 7.399 \times 10^{-6}$$

Before we got 7.45×10^{-6}



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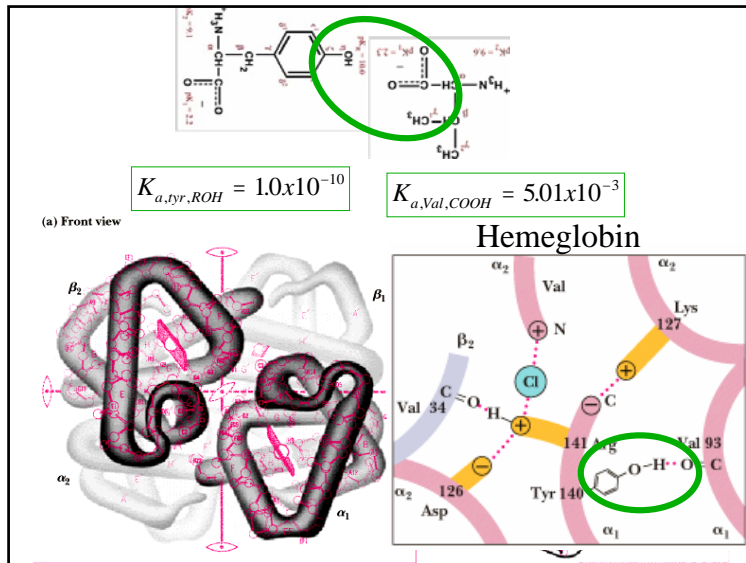
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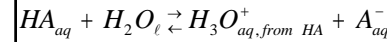
Module #17B:
Acid Base Ionization
Computations

Biological Chemistry

- Example Calculations
1. HCl
 2. Acetic acid (vinegar)
 3. HF
 4. B(OH)₃ (Boric acid (eye wash)) (students Do this one yourself)
 5. Mixture (HF and phenol)
 6. Mixture (H₂SO₄, HSO₄⁻)
 7. Triethylamine
 8. NaAcetate
 9. Our heme example



Which pH (2, 7, 11) is most favorable for the formation of a hydrogen bond between Val and tyr in hemoglobin assuming that we define favorable as having the most possible H bonds.



$$K_{a,Val,COOH} = 5.01 \times 10^{-3}$$

$$K_{a,tyr,ROH} = 1.0 \times 10^{-10}$$

$$\% \text{ dissociated} = 100 \frac{[A^-_{aq,eq}]}{[HA_{mit}]}$$

$$K_a = \frac{[A^-_{aq,eq}][H_3O^+_{aq,eq}]}{[HA_{eq,eq}]}$$

Mass balance

$$\frac{[A^-_{aq,eq}][H_3O^+_{aq,eq}]}{K_a} = [HA_{eq,eq}]$$

$$[HA_{mit}] = [HA_{eq,eq}] + [A^-_{aq,eq}]$$

$$\% \text{ dissociated} = \frac{100[A^-_{aq,eq}]}{[HA_{eq,eq}] + [A^-_{aq,eq}]}$$

$$\% \text{ dissociated} = \frac{100[A^-_{aq,eq}]}{\frac{[A^-_{aq,eq}][H_3O^+_{aq,eq}]}{K_a} + [A^-_{aq,eq}]}$$

Which pH (2, 4.7, 7, 11) is most favorable for the formation of a hydrogen bond between Val and tyr in hemoglobin assuming that we define favorable as having the most possible H bonds

$$K_{a,Val,COOH} = 5.01 \times 10^{-3}$$

$$K_{a,tyr,ROH} = 1.0 \times 10^{-10}$$

$$\% \text{ dissociated} = \frac{100[A^-_{aq,eq}]}{\frac{[A^-_{aq,eq}][H_3O^+_{aq,eq}]}{K_a} + [A^-_{aq,eq}]}$$

$$\% \text{ dissociated} = \frac{100}{\frac{[H_3O^+_{aq,eq}]}{K_a} + 1}$$

$$pH 2; [H^+] = 10^{-2}$$

$$\% \text{ dissociated COOH} = \frac{100}{\frac{[10^{-2}]}{5.01 \times 10^{-3}} + 1} = 33.33$$

Repeat procedure
With tyrosine


pH	$10^{-(pH)}$ [H ⁺]	valanine		tyrosine	
		Ka COOH	%ionized	Ka OH	%ionized
2	0.01	5.00E-03	33.33333	1.00E-10	1.00E-06
4.7	1.99526E-05	5.00E-03	99.60253	5.01E-04	5.01E-04
7	0.0000001	5.00E-03	99.998	9.99E-02	9.99E-02
10	1E-10	5.00E-03	100	5.00E+01	5.00E+01

$K_{a,tyr,ROH} = 1.0 \times 10^{-10}$ $K_{a,Val,COOH} = 5.01 \times 10^{-3}$

valanine tyrosine
Ka Ka
COOH OH
%ionized %ionized

pH	$10^{-(pH)}$ [H ⁺]	valanine		tyrosine	
		Ka COOH	%ionized	Ka OH	%ionized
2	0.01	5.00E-03	33.33333	1.00E-10	1.00E-06
4.7	1.99526E-05	5.00E-03	99.60253	5.01E-04	5.01E-04
7	0.0000001	5.00E-03	99.998	9.99E-02	9.99E-02
10	1E-10	5.00E-03	100	5.00E+01	5.00E+01

Which pH is best?
Hint: Want Val ionized
Tyr not ionized



I WANT YOU TO PRACTICE EVERY DAY!

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**Module #17B:
Acid Base Ionization
Computations**

When should we Be making assumptions?

Example on Using Simplifications **Module 17A**

If 1.0 mol NOCl is placed in a 2.0 L flask what are the equilibrium concentrations of NO and Cl₂ given that at 35 °C the equilibrium constant, K_c , is 1.6×10^{-5} mol/L?

Red herrings: 35 °C is a red herring 

Clues?
K is “small” compared to others ($\lll 1$) we have worked with !!!!!

Example 2 $CO_{2,g} + H_{2,g} \rightleftharpoons CO_g + H_2O_g$ K_c is 0.64.

EXAMPLE 3: $N_2O_4 \rightleftharpoons 2NO_{2(g)}$ $K_c = 0.36M$ **We will define Small in the Next chapter!**

Example 4: $H_{2,g} + I_{2,g} \rightleftharpoons 2HI_{(g)}$ K_p is 1×10^{-2} .

We want to know when assumptions are valid.

	HA _(aq)	H ⁺ _{from HA}	A ⁻
Init	HA _{INIT}	10 ⁻⁷	0
Change	-x	+x	+x
Equil	HA _{INIT} -x	10 ⁻⁷ +x	x

$$K_a = \frac{(x)(x + 10^{-7})}{[HA_{INIT}] - x} \approx \frac{x^2}{[HA_{INIT}]}$$

$$\left(\frac{x}{[HA_{init}]} \right) 100 < 5\% ???$$

↑
%ionized

The issue is small Ka with respect To the initial concentration!!

Considering a simple system

$$HA_{eq} \rightleftharpoons A_{eq}^- + H_{eq}^-$$

Mass balance $[A_{aq,eq}^-]^2 = [HA_{aq,eq}]K_a$

$$[HA_{init}] = [HA_{eq,eq}] + [A_{aq,eq}^-]$$

$$[A_{aq,eq}^-] = \sqrt{[HA_{eq,eq}]K_a}$$

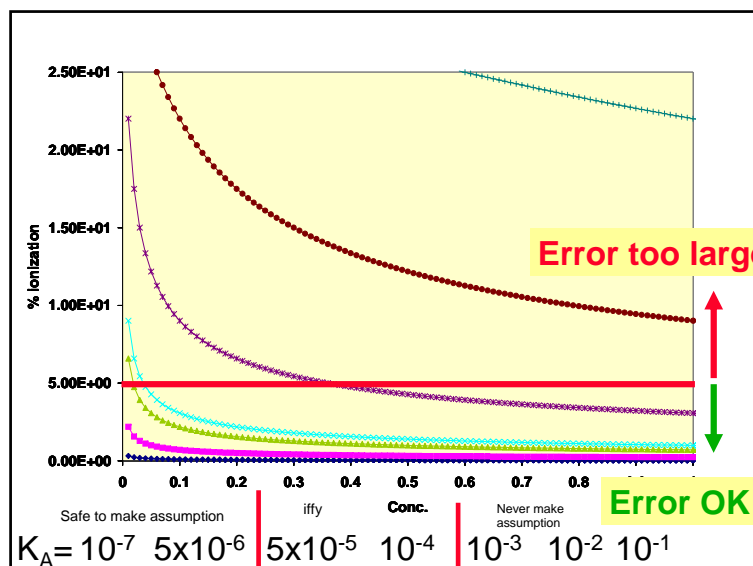
$$\% \text{ dissociated} = \left(\frac{[A_{aq,eq}^-]}{[HA_{eq}] + [A_{aq,eq}^-]} \right) 100$$

$$\% \text{ dissociated} = \left(\frac{\sqrt{K_a [HA_{eq}]}}{[HA_{eq}] + \sqrt{K_a [HA_{eq}]}} \right) 100$$

$K_a = \frac{[A_{aq,eq}^-][H_3O_{aq,eq}^+]}{[HA_{eq,eq}]}$

**OK this is not a nice equation
Do you need to know it?**

$$[A_{aq,eq}^-][H_3O_{aq,eq}^+] = [HA_{eq,eq}]K_a$$



Rule of Thumb

Small $K \sim < 10^{-6}$

Sort of small $10^{-6} < K < 10^{-4}$

Large $K \sim > 10^{-3}$

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